

Team 18

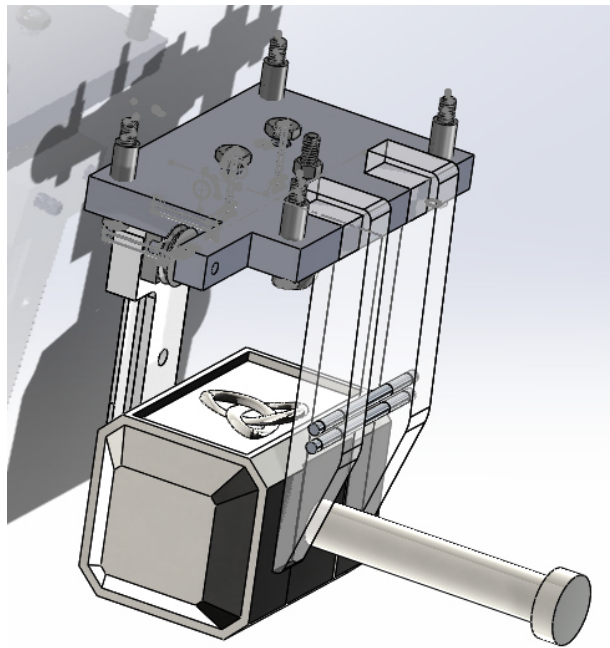
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Project 2

Final Report

11/30/2015



### **Rationale of Design:**

The design consists of a stationary wall and a movable wall that clamp the hammer. These walls are attached to a mounting plate connected half an inch directly below the robot wrist. The mounting plate is a thin acrylic sheet designed to simplify assembly to the robot wrist and also minimize the length of the walls.

A 3D printed ABS spool is connected to the driveshaft. The spool has two shafts of different diameters to connect to two 65lb strength fishing lines. The first string attached to the smaller diameter shaft is used to clamp the hammer. The second string is attached to the larger diameter and brings the movable wall to its initial position when the motor is in reverse.

Our stationary wall is two acrylic prongs that have two thin aluminum rods running through them. The clamping string runs around each rod to generate normal force. With two walls, they share the tension force through the rods and therefore can be thinner.

Our movable wall has an I-beam cross section. This allows us to maximize the area moment of inertia, which minimizes bending stress in the wall and allows us to minimize mass. The movable wall has an eye bolt in the center to connect to the clamping string. The eye bolt is placed on the lowest point on the wall that does not interfere with the hammer. The low eye bolt placement allows for the highest normal force from contact with the hammer. We also used football “Cutter” gloves on all of the walls because it generated the highest coefficient of friction between the walls and the hammer.

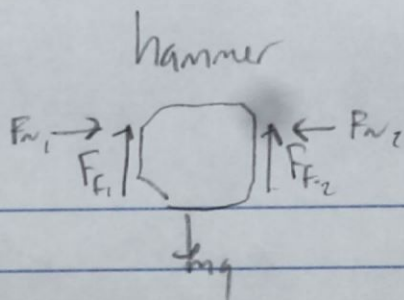
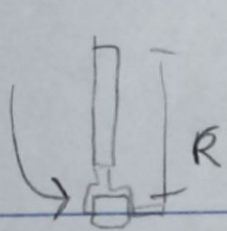
**Peak Force:** 9.91 lbs for each wall (Page 3)

**Factor of Safety for Grip:** 1.634 (Page 5)

**Factor of Safety Strength:** 1.096 (Page 9)

### **Weakest Component:**

We believe our weakest component will be our movable wall. Due to the complexity of the design we had to 3D print it out of ABS Plastic, which has a lower yield strength compared to acrylic and aluminum, which are used for other materials in our design. We therefore believe failure would occur due to bending at the center point where the eye-hook is.



①  
Peak force  
calculation

by symmetry:  $F_{N1} = F_{N2}$   
 $\Rightarrow F_{f1} = F_{f2}$  (same  $\mu$ )

$$\sum F_y = 0 = 2F_f - mg = \frac{mv^2}{R}$$

$$\therefore 2F_f - mg = \frac{m \frac{v_{\max}^2}{2R}}{R}$$

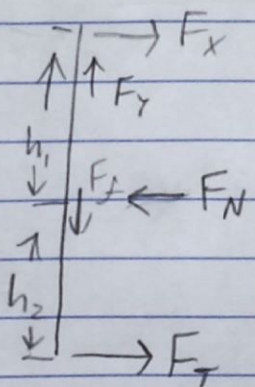
so need  $F_f$  max

$2F_f = 3mg \Rightarrow$  total friction force needed  
 each wall needs  $F_f$  of  $1.5mg$

total upward force needed for hammer:  $44.10 \text{ N} = 9.91 \text{ lbs} = F_p$

each wall has  $\mu = 0.5$  and equal  $F_N$

$$F_N \text{ each wall} = 44.10 \text{ N}$$



$$\sum M_h = 0 = F_N \cdot h_1 + F_T \cdot (h_1 + h_2)$$

$$F_T = \frac{F_N \cdot h_1}{h_1 + h_2}$$

$$h_1 = 2.25 \text{ in}$$

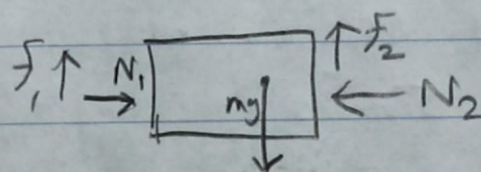
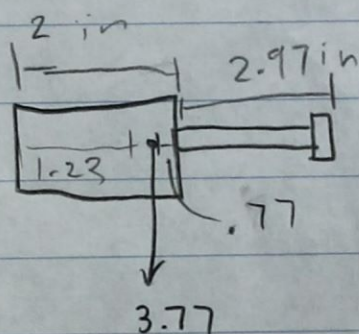
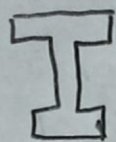
$$h_2 = .25 \text{ in}$$

$$F_N = 44.1 \text{ N} = 9.91 \text{ lbs}$$

$$F_T = 8.919 \text{ lbs}$$

Tension force required





$$\sum M_1 = -mg(0.031) + f_2(-0.0769)$$

$$\sum F_y: f_1 + f_2 - mg = m \frac{v^2}{r} \quad f_2 = \frac{mg(0.031)}{(-0.0769)}$$

$$f_1 = 38.118 \text{ N}$$

$$f_2 = 5.9258 \text{ N}$$

$$V =$$

$$\Delta V_c = 0$$

$$\Delta V_g: V_{g1} = -mg(28)$$

$$V_{g2} = 0$$

$$\Delta T: T_1 = 0$$

$$T_2 = \frac{1}{2}mv^2 (m_H + m_{gr})$$

$$\frac{1}{2}mv^2 = mg(28)$$

$$(m_H + m_{gr})$$

$$28 \text{ in} = 0.7112 \text{ m}$$

$$v^2 = 2g(28)$$

$$v = \sqrt{2g(0.7112)}$$

$$v = 3.73 \text{ m/s}$$



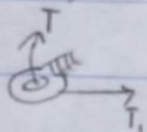
# Tension Generated

$\mu$  for nylon-aluminum = 0.22

$$T_f = T_e^{-\mu\beta} \quad \beta = \text{angle of string}$$

$$T = 49.17 \text{ lb}$$

First eye-hook

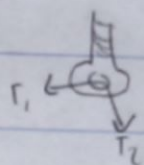


$$\beta = 90^\circ$$

$$T_1 = T_e^{-\mu\beta} = 49.17 e^{-0.22(\pi/2)}$$

$$T_1 = 34.80 \text{ lb}$$

Mounting Plate eye-hook



$$\beta = 90^\circ$$

$$T_2 = T_1 e^{-\mu\beta} = 34.80 e^{-0.22(\pi/2)}$$

$$T_2 = 24.6 \text{ lb}$$

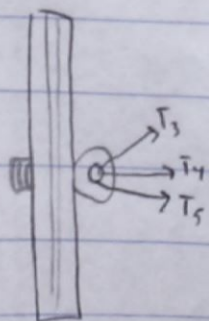
Then goes through 3 180° loops on aluminum bars / eye hooks

$$T_3 = T_2 e^{-\mu\beta} = 24.6 e^{-0.22(\pi)} = 10.2 \text{ lb}$$

$$T_4 = T_3 e^{-\mu\beta} = 10.2 e^{-0.22(\pi)} = 4.2 \text{ lb}$$

$$T_5 = T_4 e^{-\mu\beta} = 4.2 e^{-0.22(\pi)} = 1.6 \text{ lb}$$

movable wall

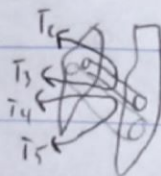


$$F_T = T_3 + T_4 + T_5$$

$$= 16.2 \text{ lb}$$

$$F.O.S. = 1.634$$

stationary wall



$$F_T \text{ per wall} = \frac{T_2 + T_3 + T_4 + T_5}{2}$$

$$= 20.4 \text{ lb}$$

$$F.O.S. = 2.05$$

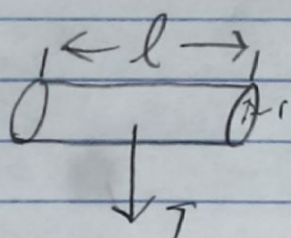
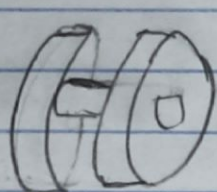


②

Finding Tension force of fishing line from spool

First must find minimum possible diameter of spool so the maximum tension is obtained from torque of motor but not small enough that ABS fails.

Max force experience in inside of spool is bending at the edges



$l$  is known  
 $T = \frac{\tau \leftarrow \text{Torque from motor}}{r}$

$$\tau = 1.1 \text{ N}\cdot\text{m} = 9.736 \text{ lb}\cdot\text{in}$$

$$EM_{\text{edge}} = \frac{Tl}{2}$$

$$\sigma = \frac{My}{I} = \frac{Tl/2 \cdot r}{\frac{\pi r^4}{4}} = \frac{2\tau l}{\pi r^3}$$

$I$  of circle C.S. =  $\frac{\pi r^4}{4}$

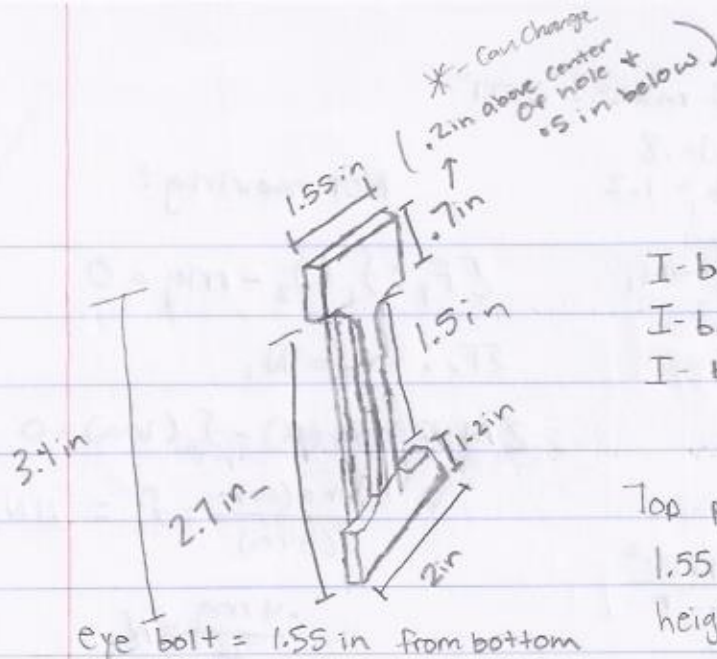
For ABS  $\sigma_y = 7000 \text{ lb/in}^2$

$$\sigma = \frac{\sigma_y}{\text{F.O.S}} \quad \text{say for now that F.O.S} = 10$$

$$r = \left( \frac{2\tau l}{\pi} \cdot \frac{\text{F.O.S}}{\sigma_y} \right)^{1/4}$$

$$r = .1981 \text{ in}$$

$$\therefore T = \frac{\tau}{r} = \boxed{49.17 \text{ lbs}}$$



I-beam depth (overall h) = .4 in  
 into page

I-beam width (b) = .7 in

I-beam length = 2.7 in \* - figure  
 out something  
 for screws

Top part Hinge attaches to:

1.55 in = width

height = .7 in ← \* - may change

eye bolt = 1.55 in from bottom

holes for screws: 3.2 in from  
 bottom

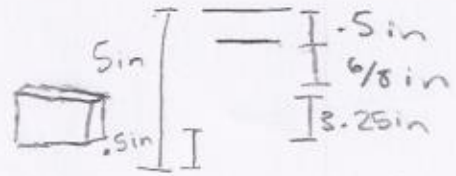
bottom plate:

1.2 in high

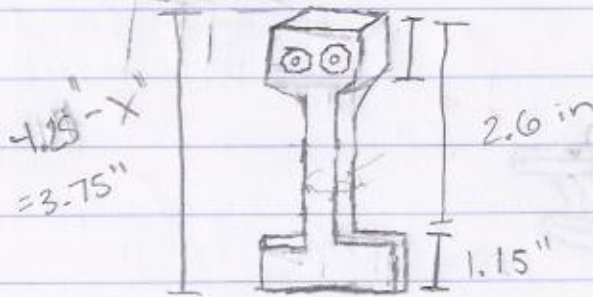
2 in wide



Arm length = 3.2 in  
 $X = .5$  in Face = 1.2 in



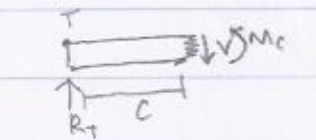
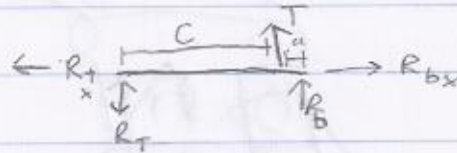
$X$  = height plate dropped down



$$A = Wh$$

$T$  = String tension

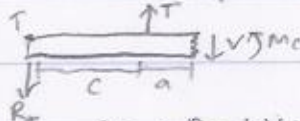
$$I_{rec} = \frac{1}{12} bh^3$$



$$\sum F_y: V = R_T$$

$$\sum M: -R_T C + M_C = 0$$

$$M_C = R_T C$$



$$\sum F_y: R_T + V = T$$

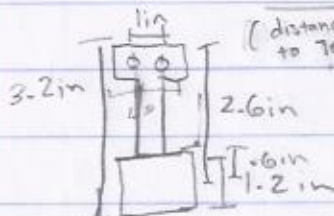
$$\sum M: R_T(C) - T(a) + M_C = 0$$

bending Stress:  $\sigma_{max} = \frac{M_{max} \frac{h}{2}}{\frac{1}{12} bh^3} = \frac{6 M_{max}}{bh^2}$

Max Shear Stress:  $\frac{V_{max}}{A} = \tau_{max}$

$$\sigma_{max} = \frac{\sigma_y}{FS}$$

$$T = N_H \left( \frac{\text{distance to } N_H}{N_H} \right)$$

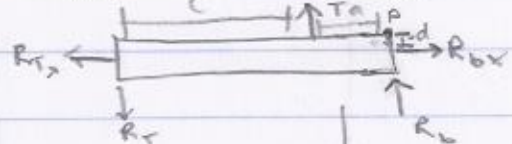


$$\sum F_y: T + R_B = R_T$$

$$\sum F_x: R_{Tx} = R_{Bx}$$

$$\sum M_B: T(a) = R_{Tx}(C + a)$$

$$\text{Axial Stress} = \frac{R_{Tx}}{A} = \frac{R_{Bx}}{A}$$



$$\sum M_P: R_T(c+a) + R_{Tx}(d) - T(a) + R_{Bx}(d) = 0$$

$$R_{Tx} = \frac{R_T(c+a) - T(a) + R_{Bx}(d)}{(d)}$$



bending stress max

$$\sigma_{max} = \frac{M h/2}{\frac{b h^3}{12}} = \frac{6 M_{max}}{b h^2}$$

$$(2053.73) = \frac{6(35)}{b h^2}$$

$$b h^2 = .022$$

IF  $b = .7 in$   
 $h = .388 in$

$$\sigma_m = 14.16 MPa$$

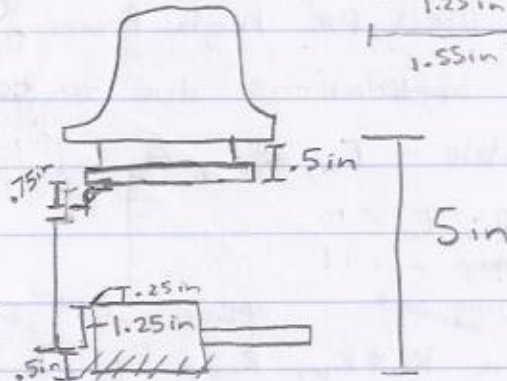
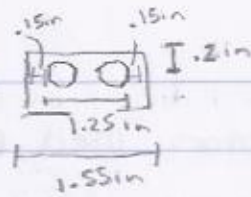
$$= 2053.73 PSI$$

$$FS = 3$$

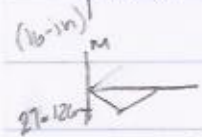
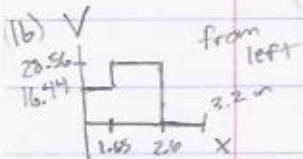
$$\frac{\sigma_y}{\sigma_m} = FS$$

ABS plastic

$$\sigma_y = 42.5 MPa$$

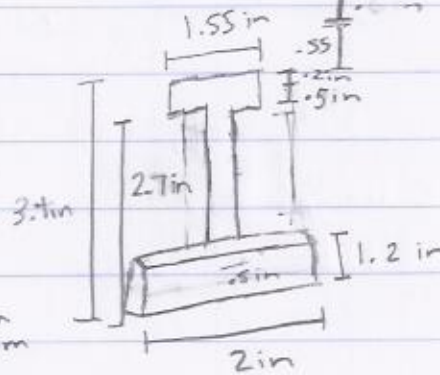


$$x = 3.4 in$$



assume max moment is 35 lb-in = 4 N-m

Max Moment = 27.126 lb-in



$$T = 45 lb = 200.16 N$$

$$\sum F_y: T = R_T + N_H$$

$$\sum M_H: T(-.95 in) = R_T(2.0 in)$$

$$R_T = 16.44 lb = 73.12 N$$

$$N_H = 28.56 lb$$

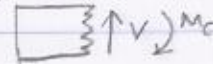
$$= 127.09 N$$

$$\sum F_y: T - N_H - R_T = 0$$

$$\sum M_C: R_T(3.2) - T(1.55) + N_H(.6) = M_C = 0$$

$N_H$  is .6 in from end of bar

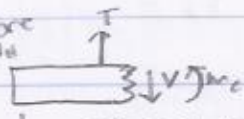
Before  $T$ :



$$\sum F_y: V = R_T$$

$$\sum M: M_C = R_T(1.65)$$

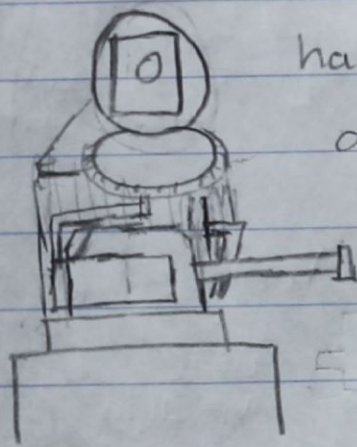
Before  $N_H$ :



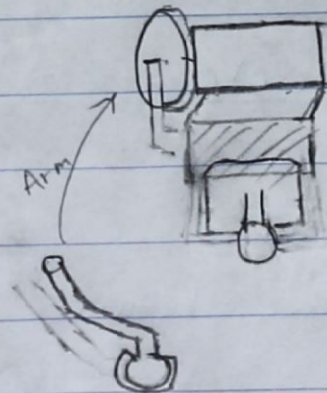
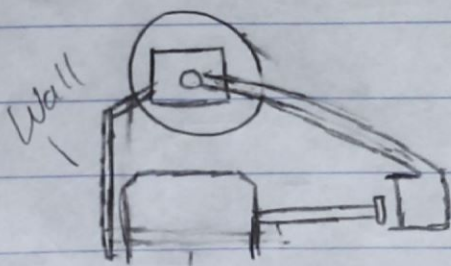
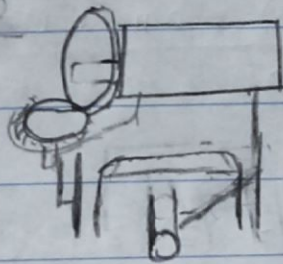
$$\sum F_y: T - R_T = V$$

$$\sum M: M_C = -R_T(2.6) + T(.95)$$

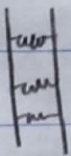
10 11  
 Note top of the Hammer



Front like arm that moves  
 hammer towards back wall  
 and Squeezes hammer



maybe wall



Springs  
 that when  
 compressed  
 want to return  
 to rest



# Optimizing the fixed wall

1st. Optimize structure for type of loading to be experienced

Center of pressure on same line as COM

Equidistant on both sides of the handle

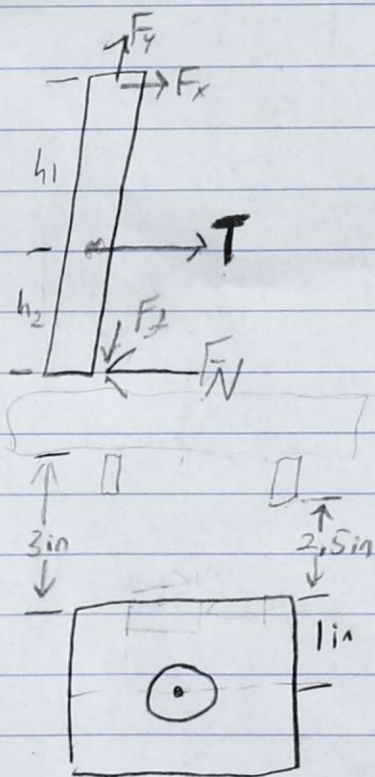
Minimum surface area while making sure contact force isn't too high

Select ideal material

Options:

- ABS ( $\sigma_s = 6160-6500 \text{ psi}$ ) ( $\rho = .0376 \text{ lb/in}^3$ )

- Acrylic ( $\sigma_s = 10000 \text{ psi}$ ) ( $\rho = .04 \text{ lb/in}^3$ )



$$\sum M_{I_k} = h_1 T - F_N h_2 = 0$$

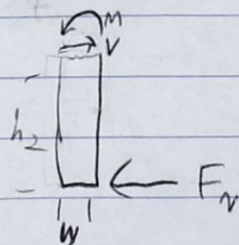
$$F_N = \frac{3mg}{\mu} \quad \text{Calculated based on Normal}$$

$$T = \frac{F_N(h_2 + h_1)}{h_1} \quad \text{force required}$$

$$T = \frac{3mg h_2}{\mu h_1}$$

$$h_1 \approx 2.4 \text{ in} \quad h_2 \approx 1 \text{ in}$$

$$t_{\text{acrylic}} = .173 \text{ in} \quad t_{\text{ABS}} = ?$$



$$M = F_N h_2$$

$$\sigma = \frac{My}{I}$$

$$\sigma = \frac{F_N h_2 \cdot w/2}{t w^3 / 12} = \frac{F_N h_2 6}{t w^2}$$

$$mg = 3.308 \text{ lbs}$$

$$F.O.S = 5$$

$$w = \sqrt{\frac{F.O.S \cdot 3mg \cdot h_2 \cdot 6}{t \sigma_y 2 \mu}}$$

$$w = .435 \text{ in for acrylic}$$

$$1.77 \text{ in}$$

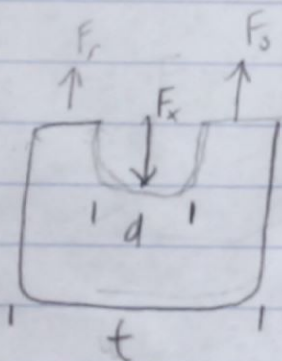


Analysis if chose to screw fixed wall to mounting plate.

$$F_x = \frac{F_N(h_z + t_w)}{L_1} F_N = 4.5485 \text{ lbs}$$

thickest acrylic = .375 in

$w = .2955 \text{ in}$



$$F_s = 1/2 F_x$$

$$\sigma = \frac{F}{A}$$

Assume  $k_t \approx 2.2$

Must account for  $k_t$  and cyclical loading

$$\sigma = \frac{\sigma_y}{F.O.S \cdot k_t}$$

$$F.O.S = 5 \quad k_t = 2.2$$

$$\sigma_y = 10000$$

$$\sigma = 909.1 \text{ psi}$$

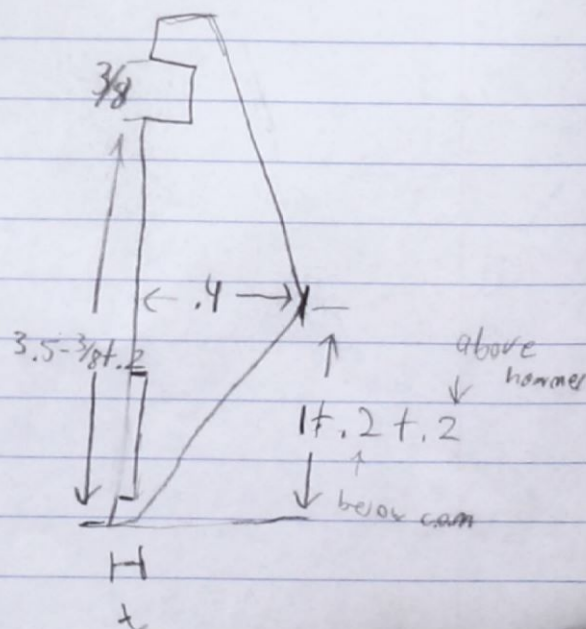
$$A = (w - d) \cdot t \quad F = 1/2 F_x$$

Assume  $d$  to be  $1/16$  set screw

$$909.1 = \frac{1/2 F_x}{(t - d) \cdot w}$$

$$w = .008 \text{ in}$$

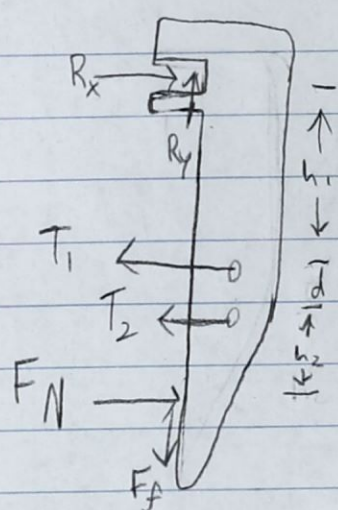
Think about tension and no normal force situation.





# Analyzing Normal force based on tension from strings

Fixed wall slip fit and acrylic glued to mounting plate



$$\sum M_R = 0 = F_N \cdot (h_2 + d + h_1) - T_1(L_1) - T_2(d + h_1)$$

From analysis done on another page for tension loss

$$T_2 = 14.4 \text{ lbs}$$

$$T_1 = 9.8 \text{ lbs}$$

$$h_1 = 2.2 \text{ in}$$

$$d = .2 \text{ in}$$

$$h_2 = .9 \text{ in}$$

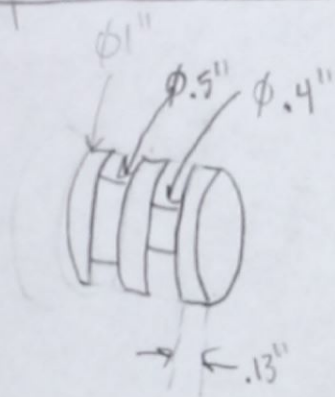
$$F_N = 17.01 \text{ lbs}$$

$$F_f = \mu F_N$$

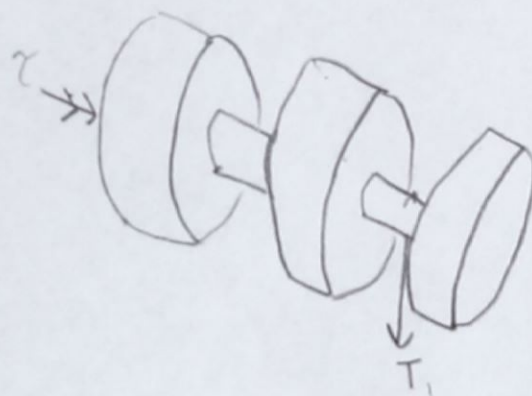
$$\mu = .5$$

$$F_f = 17.01 \cdot .5 = 8.5 \text{ lbs}$$

# Spool calculations



When motor turned on:



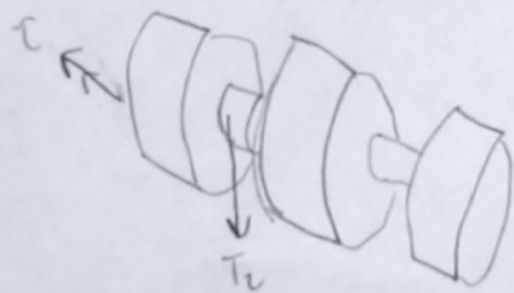
$$\sum M_{center} = 0$$

$$\tau - T_1 (.2") = 0$$

$$T_1 = \frac{\tau}{.2"} = \frac{1.3 \text{ N}\cdot\text{m}}{.2"} = 6.5 \text{ N}$$

$$T_1 = \frac{1.3}{.00509 \text{ m}} = 256 \text{ N}$$

When motor reversed:



$$\sum M_{center} = 0$$

$$-\tau + T_2 (.25") = 0$$

$$T_2 = \frac{\tau}{.25"} = \frac{1.3 \text{ N}\cdot\text{m}}{.25"} = 5.2 \text{ N}$$

$$T_2 = 204.7 \text{ N}$$

$$\sigma_{y \text{ ABS } 30 \text{ psi}} \approx 36 \text{ MPa}$$



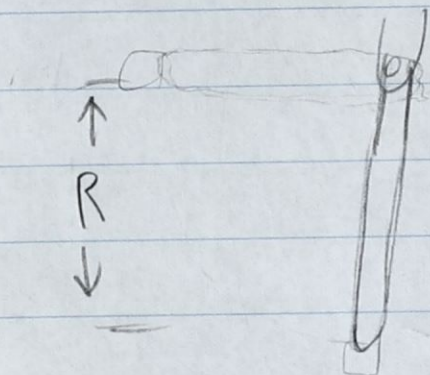
# Miscellaneous

Beginning calculations on force required from the gripper due to the swing of the robotic arm and the weight of the hammer.

Driving Torque =  $1.3 \pm .2 \text{ N}\cdot\text{m}$

max speed  $13 \frac{\text{rad}}{\text{s}}$

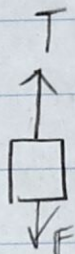
W



$$PE_1 = KE_2$$

$$mgh = \frac{1}{2}mv^2$$

$$\sqrt{2gh} = v$$

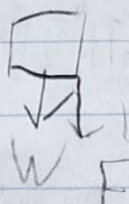


$$T = \frac{mv^2}{R}$$

highest at the bottom

$$F = \frac{2gRm}{R}$$

$$F = 2gm$$

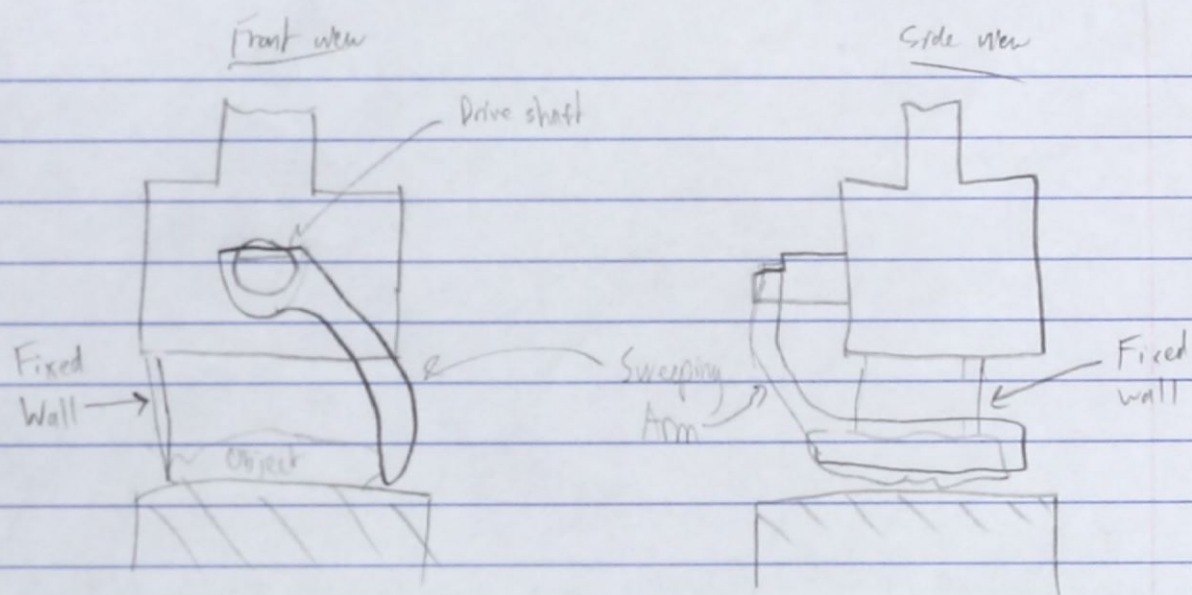


$$F = 3gm$$

Total force going down that we must counteract

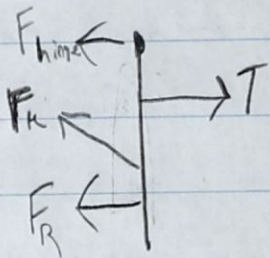


# Miscellaneous





highest possible Force from rotating wall to fixed wall

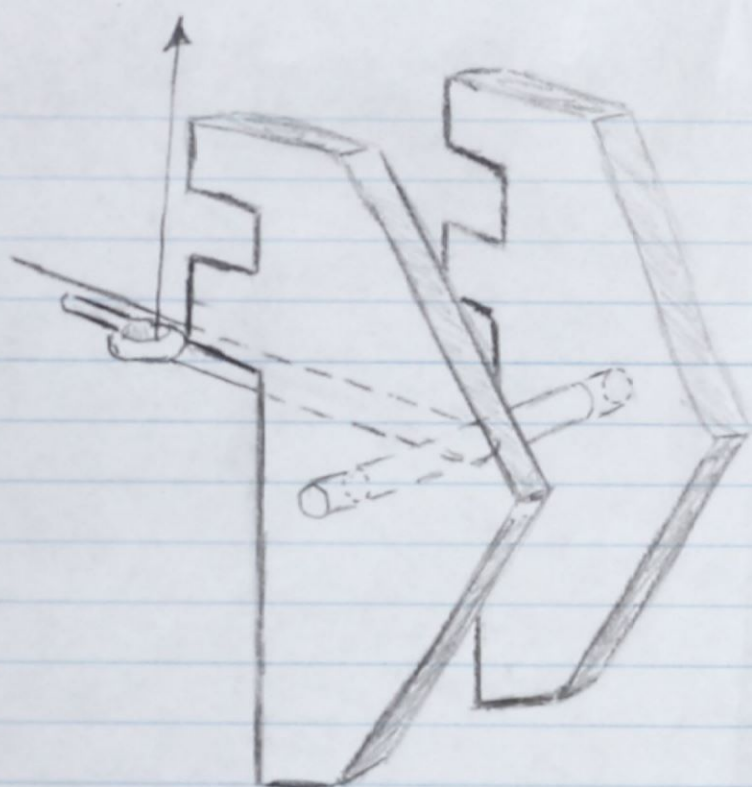


$$T_2 = T_1 e^{\mu_s \beta} \text{ angle}$$

$\mu$  and  $N$   
material selection      string location

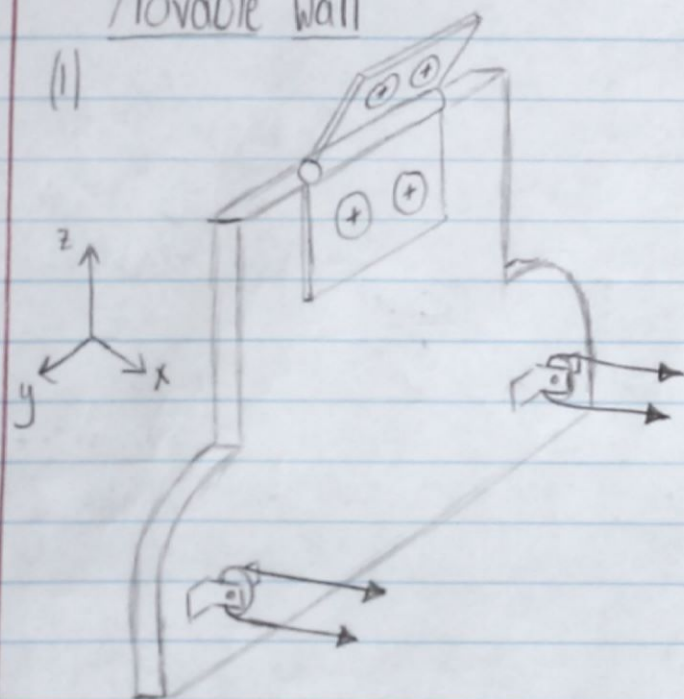


Miscellaneous



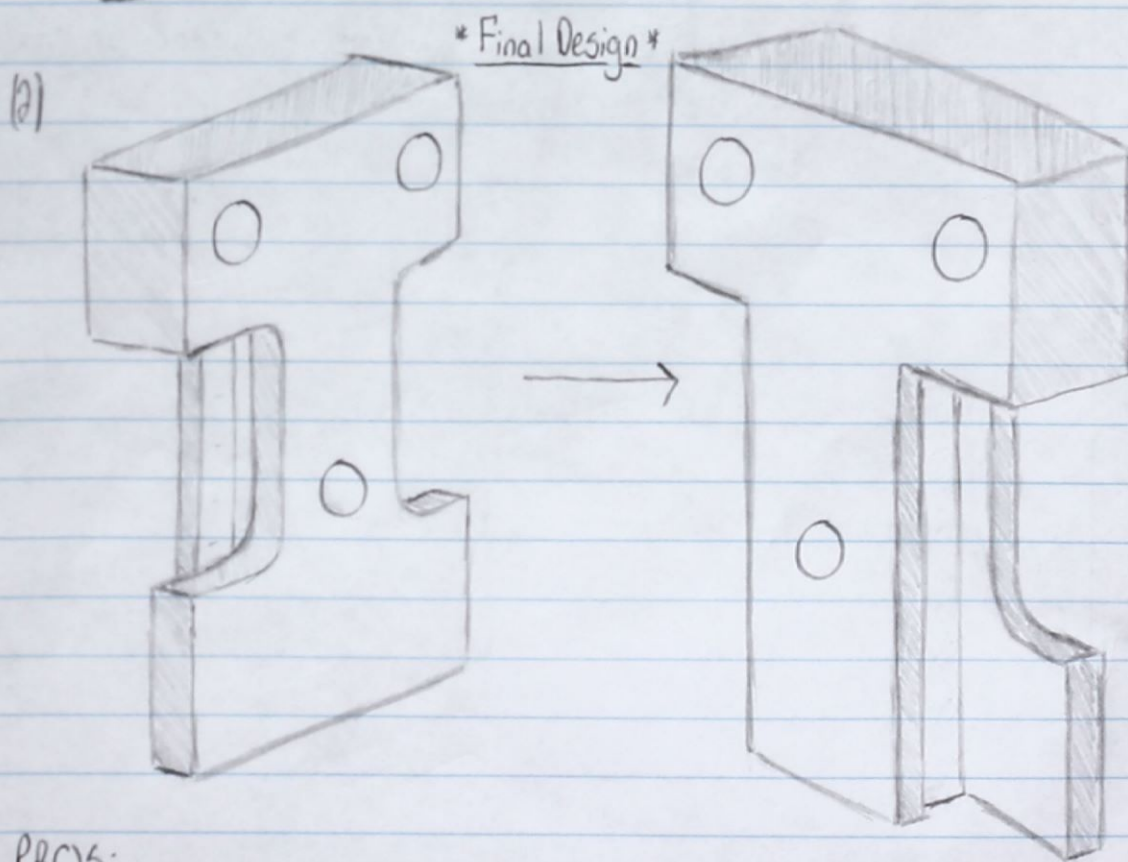


## Movable Wall



### PROS:

- Large mass
- Tension differences cause moment about z-axis  
↳ created unequal pressure
- Unoptimized geometry for bending stress



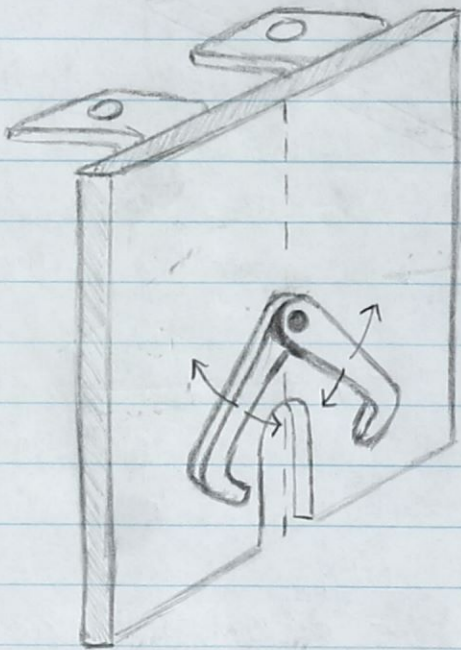
### PROS:

- Minimal mass; lightweight material
- Optimized geometry  
↳ I-beam is optimal for bending stress experienced



## Stationary Wall

(1)



### CONS:

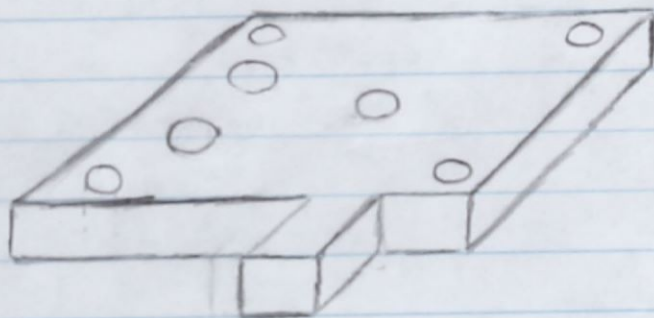
- Large mass
- Unoptimized geometry
- Too complex
  - ↳ Mechanism to move arms too complicated, scrapped that idea

### PROS:

- Provided leverage under actual object (hammer)
- Reduced required vertical friction force to reach equilibrium.



## Mounting Plate



### PROS

- lower fixed attachment surface for ports
  - ↳ movable + fixed walls

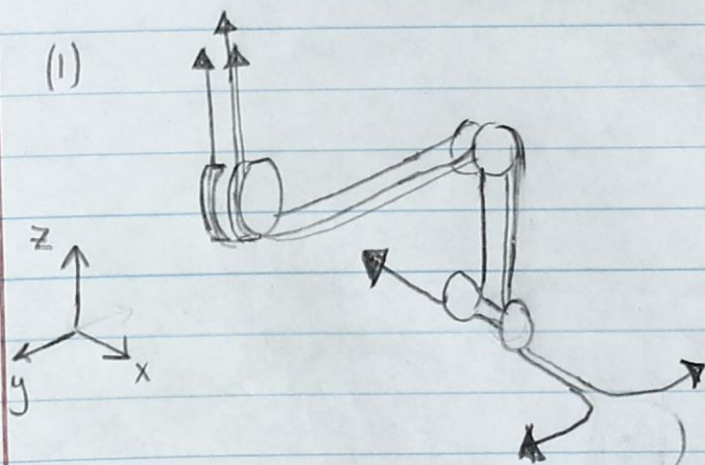
### Optimization

- Worked w/ FEA and fundamental understanding of materials to optimize:
  - thickness
  - material



# Pulley System

(1)



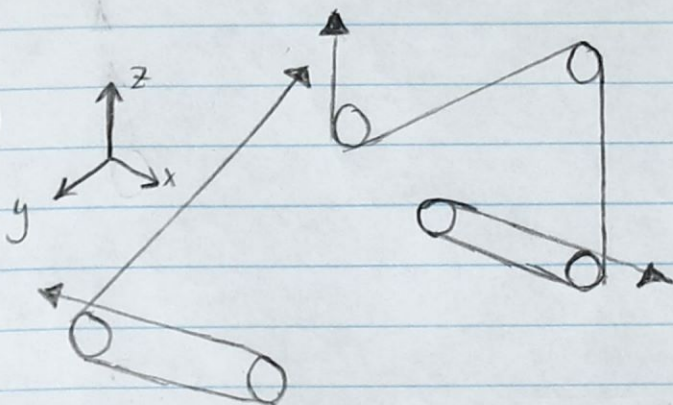
## PROS

- avoids heavy gear machinery

## CONS

- Difficult to redirect strings
- Short-circuit failure  
↳ one string pulls taught before the others and ceases mechanism

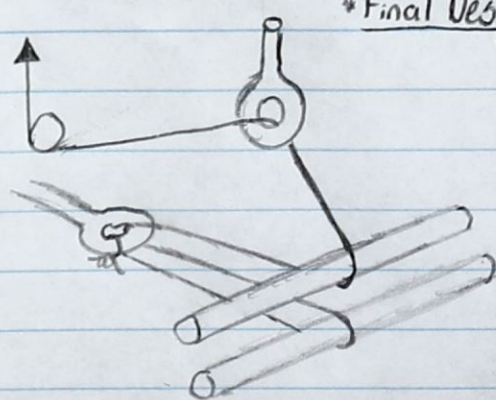
(2)



## PROS:

- Lightweight
- Takes advantage of force-length relationship in pulley system

(3)



\* Final Design \*

## CONS

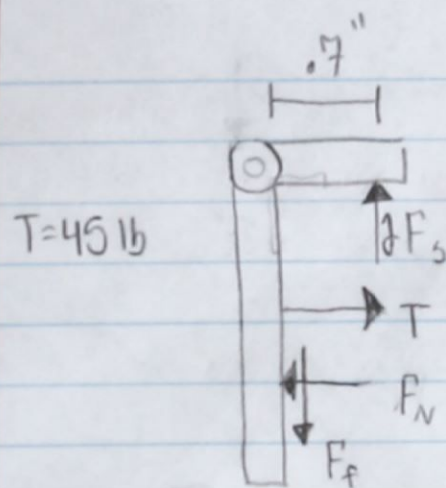
- Alignment/tensioning difficulty
- Slightly unequal force on each side, results in unequal contact  
↳ Moment about z-axis

## PROS

- Single string design (WAY EASIER)
- Still uses mechanical advantage of pulley system
- Avoids moment caused in multi-string design in (2)



# Movable Wall + Hinge



$$\Sigma F_y = 0 ; F_f = 9.90$$

$$2F_s - F_f = 0$$

$$[F_s = 4.96 \text{ lbs}]$$

Force exerted by each screw

$$\Sigma F_x = 0$$

$$F_N = T$$

$$[F_N = 45 \text{ lb}]$$

$$F_N = 45 \text{ lb} \quad F_f = 9.90 \text{ lb}$$

$$F_N =$$

## Section 5: Material Selection

**Mounting Plate – 3/8" Acrylic:** Based on the loads experienced throughout the system (mostly just vertical forces), 3/8" acrylic supported our desired factor of safety with any loads (found on page 26). We also kept changing placement of certain things on the mounting plate so it was cheaper and easier to iterate with laser cutting acrylic.

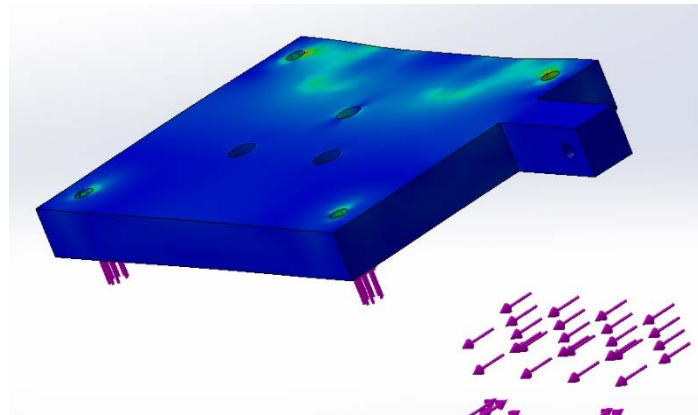
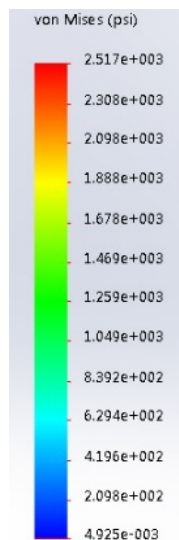
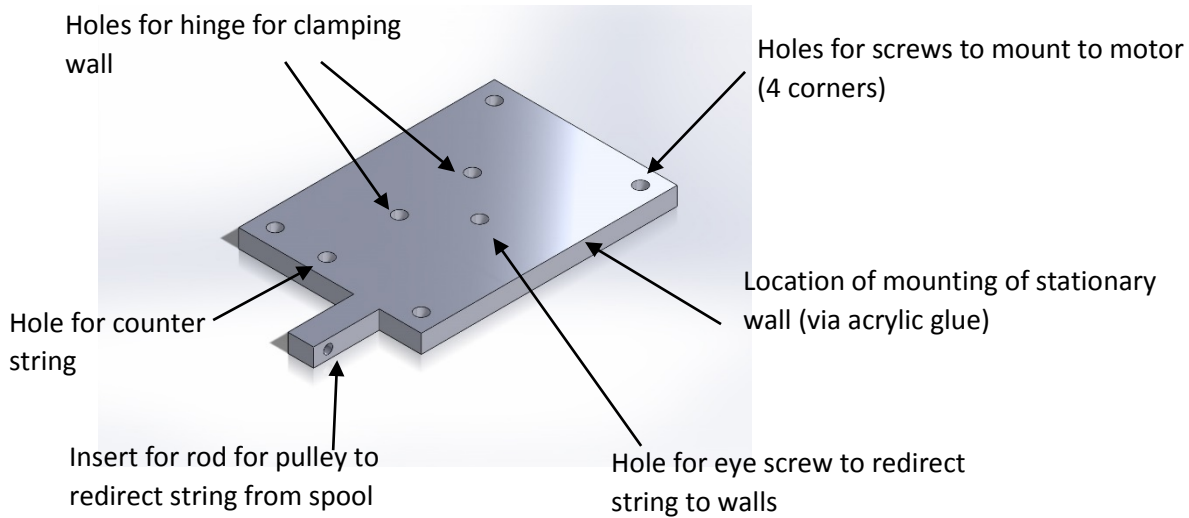
**Stationary Wall Arms (2) – 3/8" Acrylic:** Iteration of these arms were key based on different test designs we went through so laser cutting acrylic was perfect because it still had a high enough yield strength for the forces it experienced (found on page 12) and we could cut out many different parts. Since they got attached to the mounting plate we could also use acrylic glue, which reduced weight due to geometry changes and loss of screws.

**Spool – ABS Plastic:** geometry was very complex so even though we had to make the outer spool a little wider to withstand the loads (found on page 6), 3D printing a part like this is much easier, and the part is so small that cost was minimal and the additional safety length added was negligible for the weight of the entire system.

**Movable Wall – ABS Plastic:** Slightly complex geometry after optimizing to reduce weight where 3D printing was the most logical solution for manufacturing. 3D printing can also increase the strength because we can control how the layering works in our favor based on the loads applied to the part (found on page 9), making a lightweight ABS plastic a perfect choice.



## Mounting Plate Model and Analysis



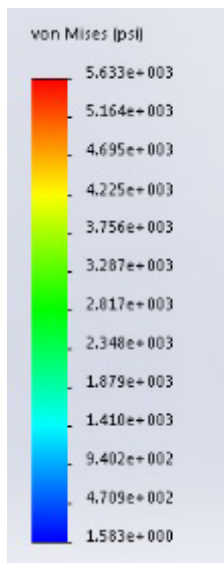
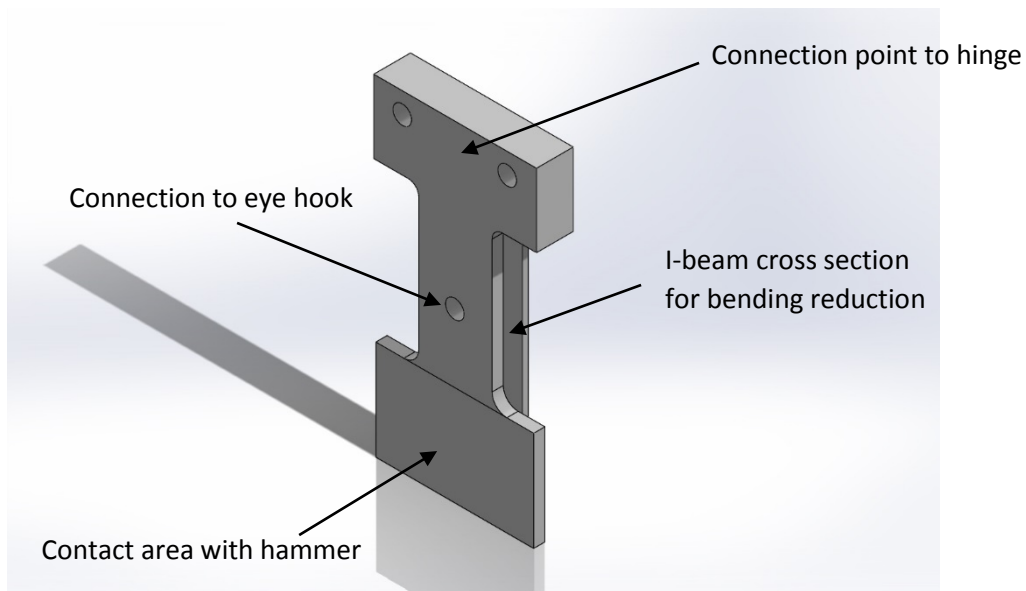
**Material:** Acrylic

**Yield Strength of Material:** 10,000 psi

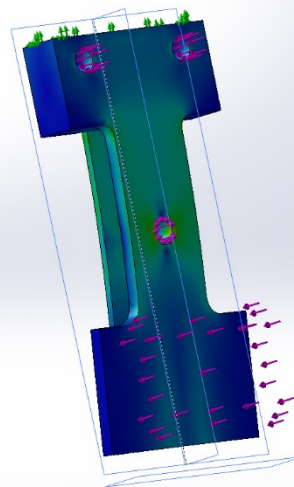
**Part Mass:** 43.76 grams

**F.O.S.:** 3.92

## Movable Arm Model and Analysis



Model name: Movable\_arm  
Study name: Static 31 (offhook)  
Plot type: Static modal stress (stress1)  
Deformation scale: 2.11475



von Mises (psi)

5.633e+003
5.164e+003
4.695e+003
4.225e+003
3.756e+003
3.287e+003
2.817e+003
2.348e+003
1.879e+003
1.410e+003
9.402e+002
4.709e+002
1.583e+000

Educational Version, For Instructional Use Only

**Material:** ABS Plastic

**Yield Strength of Material:** 6160 psi

**Part Mass:** 13.81 grams

**F.O.S.:** 1.096



## Spool Detailed Model and Analysis of Final Design

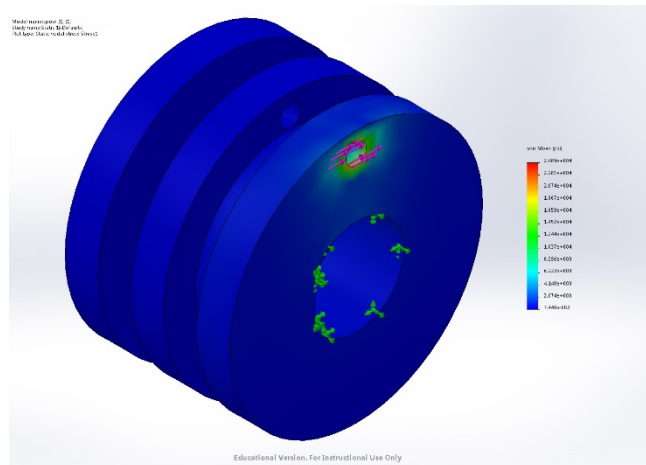
Inner diameter as small as possible to generate the most force possible in string

Holes to tie string through

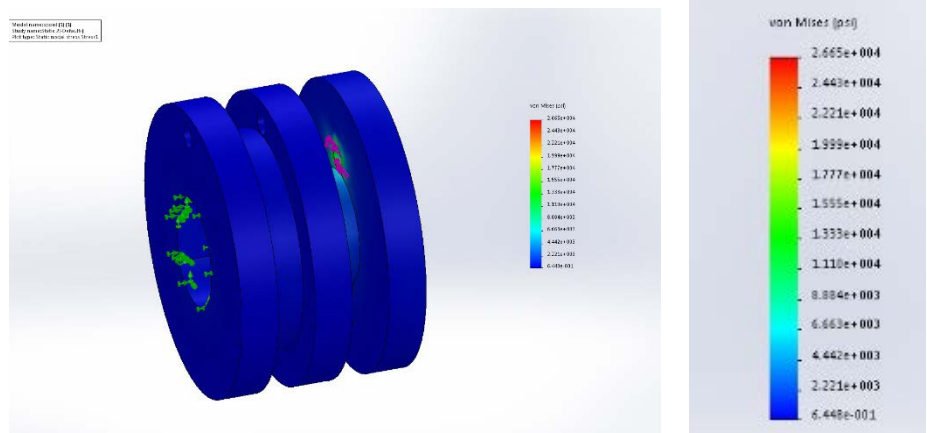
Hole cutout to fit onto motor driveshaft

Wider inner diameter for counter string to reduce force on part since not as much tension is needed

Counter string analysis



Clamping string analysis



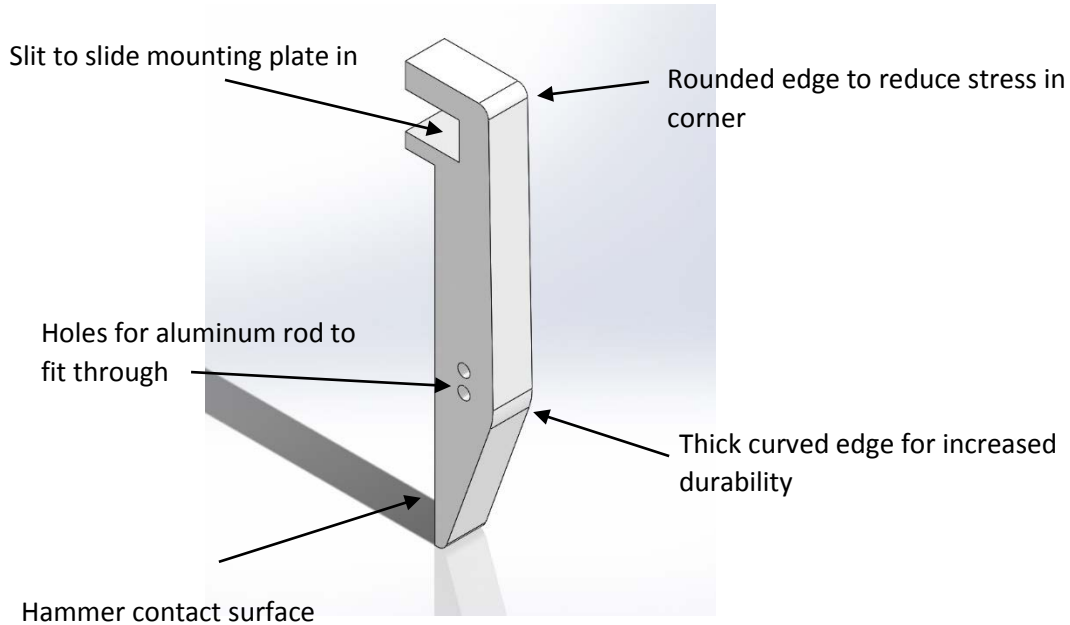
**Material:** ABS Plastic

**Yield Stress of Material:** 6160 psi

**Part Mass:** 5.84 grams

**F.O.S.:** 2.31

## Stationary Wall Model and Analysis

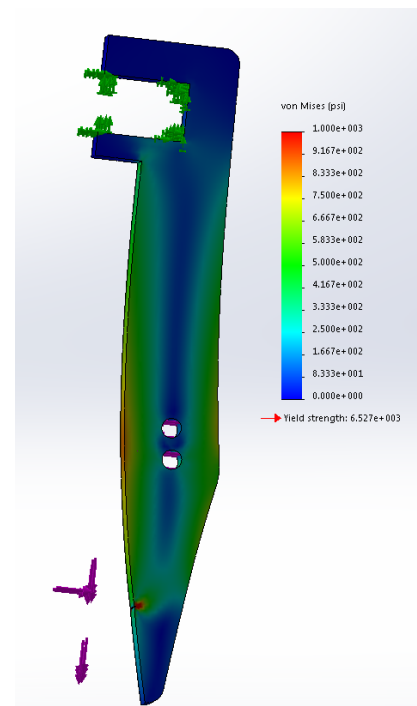
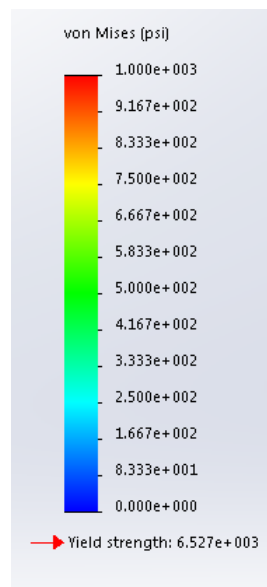


**Material:** Acrylic

**Yield Strength of Material:** 10,000 psi

**Part Mass:** 15.62 grams

**F.O.S.:** 10





## Section 7: Catalog Component Selection

**8-32 Screws:** The screws were the correct size to fit into the motor mounting plate, and were the proper length to give us our desired gap length between our mounting plate and motor. Also made it easy to remove walls from mounting plate for quick changes.

**1/8" Aluminum Bar:** gave us desired strength for being such a thin bar to hold the tensions from the strings as well as the pulley. Aluminum also had the lowest coefficient of friction with the nylon rope out of possible options so less tension was lost throughout the system.

**8-32 Nuts and Washers:** Fit the screws we were using within the system.

**1" Hinge:** Was the smallest hinge we could find for our movable wall which reduced overall weight.

**Plastic Pulley:** Smallest pulley we could find that reduced weight. Went with a little more expensive pulley because it has a built in bearing so that the pulley will spin easier, providing a smaller tension lost in the spring.

**"Cutter Gloves":** Proved to provide the greatest coefficient of friction between the wall and the hammer to increase our friction force to keep the hammer up. Were also readily available from group members on the football team.

**Spring:** provided a high enough spring constant to be able to retract our movable wall back when the tension in the string was lost, but also was short enough to fit nicely within our smaller system.

**High Strength Fishing Line:** Provided more than enough strength based on our factor of safety and was already owned by one of the group members.

**Eye Hook:** Easier to use than small pulleys. Redirected string from spool to walls and still had low enough coefficient of friction with fishing line to reduce tension lost throughout system.

**0.5" Spacers:** Kept the mounting plate at exactly the same height from the motor to ensure the walls contacted the same location of the hammer every time.

